

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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**Monday 11 May 2020**

Afternoon (Time: 1 hour 30 minutes)

Paper Reference **WFM01/01**

**Mathematics**

**International Advanced Subsidiary/Advanced Level**  
**Further Pure Mathematics F1**

**You must have:**

Mathematical Formulae and Statistical Tables (Blue), calculator

Total Marks

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**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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2. The quadratic equation

$$5x^2 - 2x + 3 = 0$$

has roots  $\alpha$  and  $\beta$ .

Without solving the equation,

(a) write down the value of  $(\alpha + \beta)$  and the value of  $\alpha\beta$  (1)

(b) determine, giving each answer as a simplified fraction, the value of

- (i)  $\alpha^2 + \beta^2$
- (ii)  $\alpha^3 + \beta^3$  (4)

(c) determine a quadratic equation that has roots

$$(\alpha + \beta^2) \text{ and } (\beta + \alpha^2)$$

giving your answer in the form  $px^2 + qx + r = 0$  where  $p, q$  and  $r$  are integers. (4)

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Question 2 continued

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Q2

(Total 9 marks)



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3.

$$f(z) = z^4 + az^3 + bz^2 + cz + d$$

where  $a, b, c$  and  $d$  are integers.

The complex numbers  $3 + i$  and  $-1 - 2i$  are roots of the equation  $f(z) = 0$

(a) Write down the other roots of this equation. (2)

(b) Show all the roots of the equation  $f(z) = 0$  on a single Argand diagram. (2)

(c) Determine the values of  $a, b, c$  and  $d$ . (5)

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**Question 4 continued**

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Q4

**(Total 9 marks)**



5. The rectangular hyperbola  $H$  has equation  $xy = 64$

The point  $P\left(8p, \frac{8}{p}\right)$ , where  $p \neq 0$ , lies on  $H$ .

(a) Use calculus to show that the normal to  $H$  at  $P$  has equation

$$p^3x - py = 8(p^4 - 1) \tag{5}$$

The normal to  $H$  at  $P$  meets  $H$  again at the point  $Q$ .

(b) Determine, in terms of  $p$ , the coordinates of  $Q$ , giving your answers in simplest form. **(4)**

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Question 5 continued

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(Total 9 marks)

Q5



6. (i)

$$\mathbf{A} = \begin{pmatrix} 1 & 0 \\ 0 & 3 \end{pmatrix}$$

(a) Describe fully the single transformation represented by the matrix  $\mathbf{A}$ . (2)

The matrix  $\mathbf{B}$  represents a rotation of  $45^\circ$  clockwise about the origin.

(b) Write down the matrix  $\mathbf{B}$ , giving each element of the matrix in exact form. (1)

The transformation represented by matrix  $\mathbf{A}$  followed by the transformation represented by matrix  $\mathbf{B}$  is represented by the matrix  $\mathbf{C}$ .

(c) Determine  $\mathbf{C}$ . (2)

(ii) The trapezium  $T$  has vertices at the points  $(-2, 0)$ ,  $(-2, k)$ ,  $(5, 8)$  and  $(5, 0)$ , where  $k$  is a positive constant. Trapezium  $T$  is transformed onto the trapezium  $T'$  by the matrix

$$\begin{pmatrix} 5 & 1 \\ -2 & 3 \end{pmatrix}$$

Given that the area of trapezium  $T'$  is 510 square units, calculate the exact value of  $k$ . (5)

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**Question 6 continued**

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Q6

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**(Total 10 marks)**









**Question 7 continued**

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**Question 7 continued**

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Q7

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**(Total 10 marks)**



8. (i) Prove by induction that, for  $n \in \mathbb{Z}^+$

$$\sum_{r=1}^n \frac{2r^2 - 1}{r^2(r+1)^2} = \frac{n^2}{(n+1)^2} \quad (6)$$

(ii) Prove by induction that, for  $n \in \mathbb{Z}^+$

$$f(n) = 12^n + 2 \times 5^{n-1}$$

is divisible by 7 (6)

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